

## Chapter 3 Linear &amp; Quadratic Functions pgs 131-179

## Objectives

1. Graph linear functions
2. Use Average Rate of Change to Identify Linear Functions
3. Determine whether a linear function is increasing/decreasing/constant
4. Build linear models from verbal descriptions

**\*\*\*RECALL:**  $m = \text{slope} = \text{rate of change} = \frac{\text{change in } y}{\text{change in } x}$  or  $\frac{\Delta y}{\Delta x}$

### 3.1 – Linear functions, their properties, & linear models

1. ) Graph Linear Functions – get into slope intercept or standard form
- $y = mx + b$   $Ax + By = C$

Example  $f(x) = -3x + 7$

What can say about the function above? What does each form allow us to do?

x intercept	y intercept (b)	slope
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Domain:

Range:

## Making a T chart for additional points

What about functions like  $f(x) = -2$

x & y intercept:

slope:

2. ) Use **Avg Rate of Change (slope)** to identify Linear functions

**ONLY** linear equations have slopes that are **CONSTANT**

x	$y = f(x) = -3x + 7$
-2	
-1	
0	
1	

Is the function below a linear function?

x	f(x)
0	0.09
1	0.12
2	0.16
3	0.22
4	0.29
5	0.39

Observation Questions:

What does changing the y-intercept do to a linear equation?

What can you conclude?

### 3. )Functions: increasing, decreasing, or constant

Slopes determine whether a linear function is increasing, decreasing, or constant.

$$(a) f(x) = 5x - 2$$

$$(b) g(x) = -2x + 8$$

$$(c) s(t) = \frac{3}{4}t - 4$$

$$(d) h(z) = 7$$

### 4. )Building Linear Models

read the story carefully - remember  $y = mx + b$

look for constant change - look for where to begin (y intercept)

write the equation in slope intercept form ( $f(x) = mx + b$ )

### STRAIGHT – Line depreciation

Book value is the value of an asset that a company uses to create its balance sheet. Some companies depreciate their assets using straight-line depreciation so that the value of the asset declines by a fixed amount each year. The amount of the decline depends on the useful life that the company places on the asset. Suppose that a company just purchased a fleet of new cars for its sales force at a cost of \$28,000 per car. The company chooses to depreciate each vehicle using the straight-line method over 7 years. This means that each car will depreciate by  $\frac{\$28,000}{7} = \$4000$  per year.

- (a) Write a linear function that expresses the book value  $V$  of each car as a function of its age,  $x$ .
- (b) Graph the linear function.
- (c) What is the book value of each car after 3 years?
- (d) Interpret the slope.
- (e) When will the book value of each car be \$8000?

[**Hint:** Solve the equation  $V(x) = 8000$ .]

- (a)
- (b)
- (c)
- (d)
- (e)



## Supply and Demand

The **quantity supplied** of a good is the amount of a product that a company is willing to make available for sale at a given price. The **quantity demanded** of a good is the amount of a product that consumers are willing to purchase at a given price. Suppose that the quantity supplied,  $S$ , and quantity demanded,  $D$ , of cellular telephones each month are given by the following functions:

$$S(p) = 60p - 900$$

$$D(p) = -15p + 2850$$

where  $p$  is the price (in dollars) of the telephone.

- (a) The **equilibrium price** of a product is defined as the price at which quantity supplied equals quantity demanded. That is, the equilibrium price is the price at which  $S(p) = D(p)$ . Find the equilibrium price of cellular telephones. What is the **equilibrium quantity**, the amount demanded (or supplied) at the equilibrium price?
  - (b) Determine the prices for which quantity supplied is greater than quantity demanded. That is, solve the inequality  $S(p) > D(p)$ .
  - (c) Graph  $S = S(p)$ ,  $D = D(p)$  and label the equilibrium price.
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(a)

(b)

(c)

